

# A Test Assembly Model for MST

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# Multistage Testing

## Development of a MST:

- Developing items
- Pretesting
- Assembly of the MST:
  - Multiple modules
  - Overlap between modules?
  - Automated Test Assembly models can be useful



# ATA models for MST

Derived from ATA for parallel tests:

- Each module is a subtest, parallel

Specifications for each module:

- TIF target
- Content, length, etc

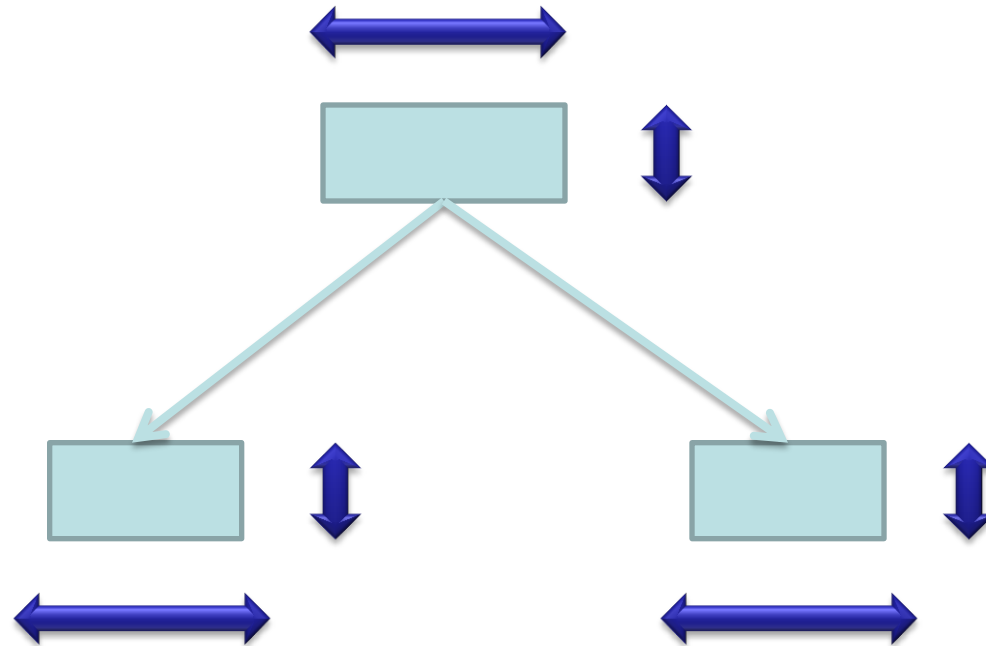
Specifications are fixed, not part of the optimization model



now you know

# ATA for MST

Specifications:



# Two problems

- What is a suitable TIF target?
- What is the optimal module length?



now you know

# TIF target

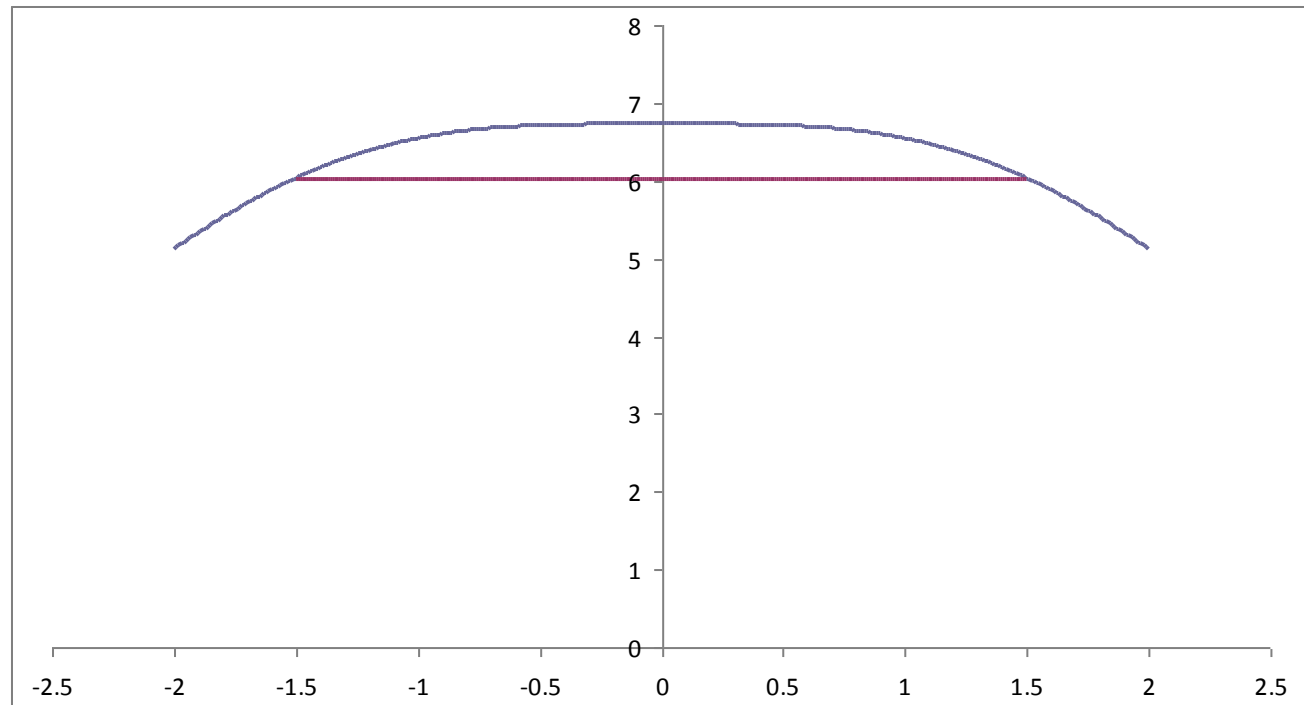
- Purpose of the test!
- Assumption:
  - ability estimation,
  - minimization of measurement error.
- Optimize TIF target, or
- Optimize constraints for ATA model



now you know

# TIF target (2)

Flat TIF target:



=> Focal points

# TIF target (3)

Flat range  $-a \dots a$ :

focal points  $-b$  and  $b$ :

$$b = 0$$

for  $a \leq \log(2 + \sqrt{3})$

$$b = \log \left( \frac{1 - 6e^{2a} + e^{4a} + \sqrt{1 - 16e^{2a} + 30e^{4a} - 16e^{6a} + e^{8a}}}{2(e^a + e^{3a})} \right)$$

for  $a > \log(2 + \sqrt{3})$

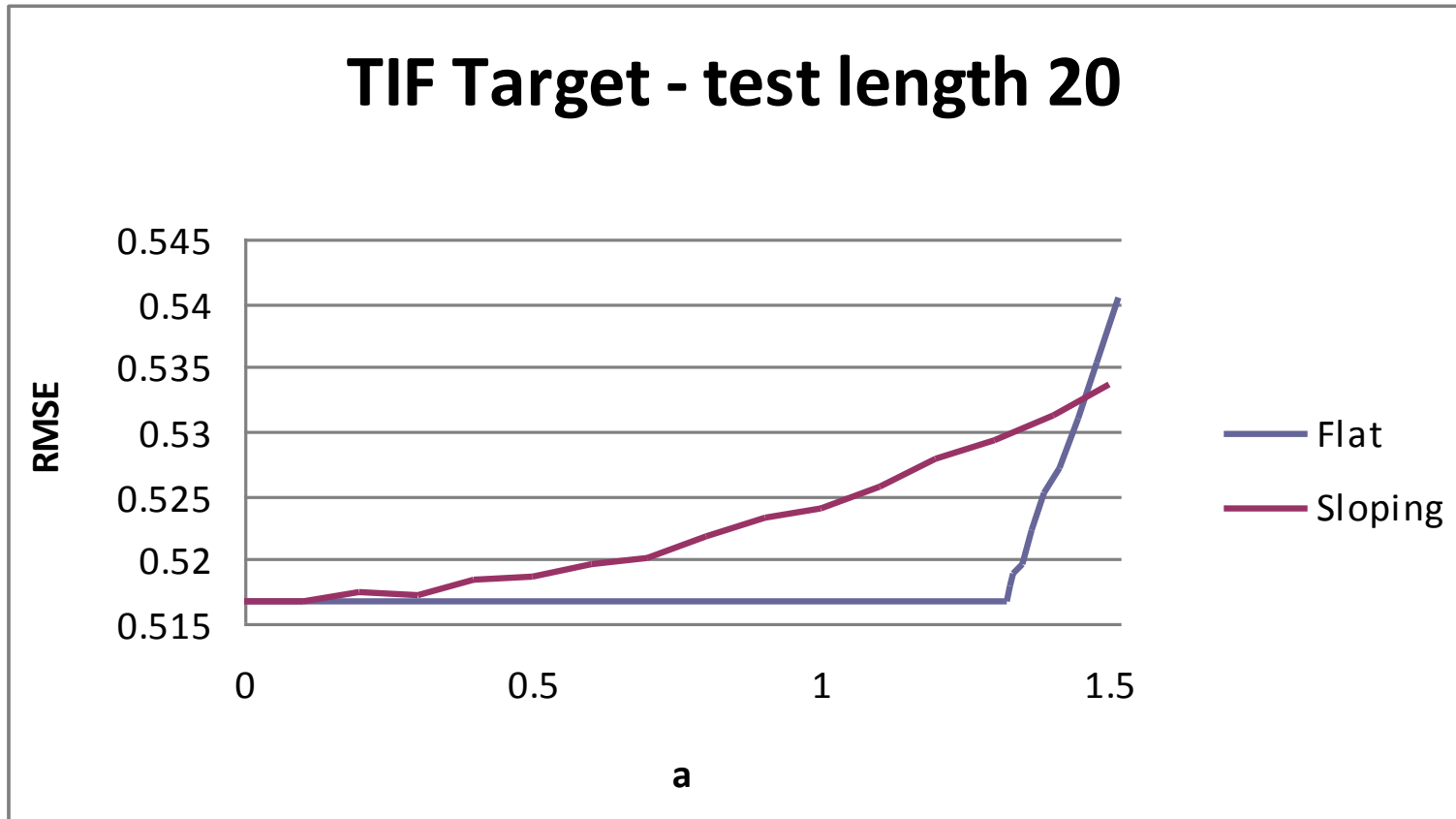
or: range of difficulties, gently sloping TIF



now you know



# TIF target (4)



# Routing

## Routing module: classification

- Minimize variance in subpopulations
  - (Roughly) equal size
  - Minimal classification error
- Routing decision based on  $\hat{\vartheta}$
- Minimization of error  $\Rightarrow$  maximization of information at decision point



# Routing: an example

Routing module: two Rasch items:

Three  $\hat{\vartheta}$  s: associated with score 0, 1, 2

Two most informative items:

70% - 30%

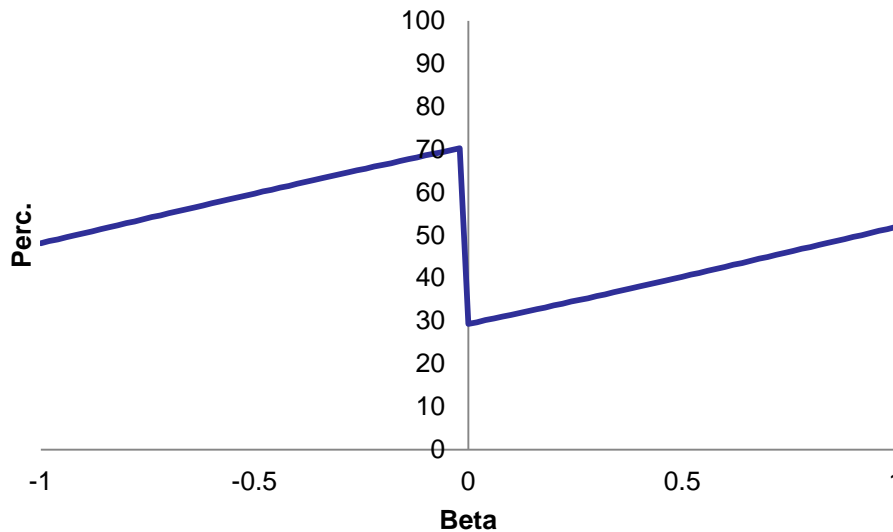
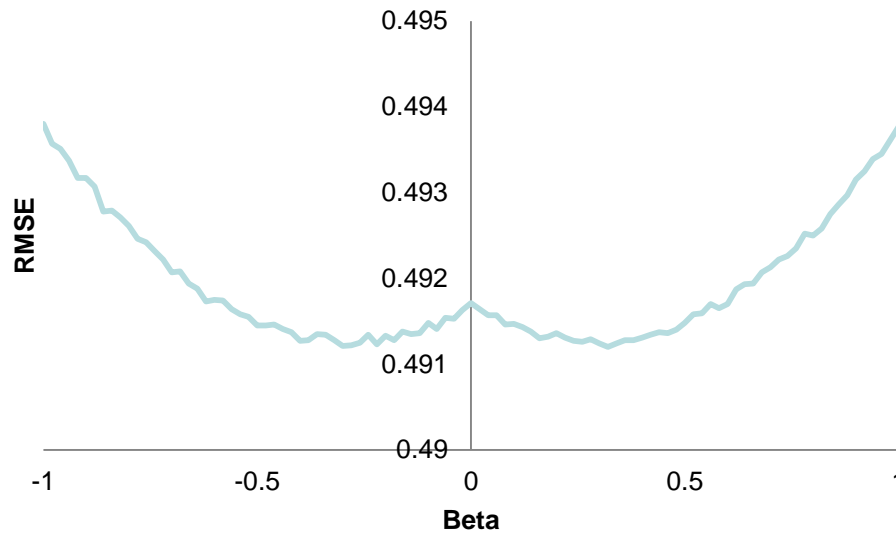
50% - 50%:

$b = -0.92$  or  $b = 0.92$



now you know

# Routing: an example (2)



# Routing Module Length

Minimization of classification error:

- extending routing module

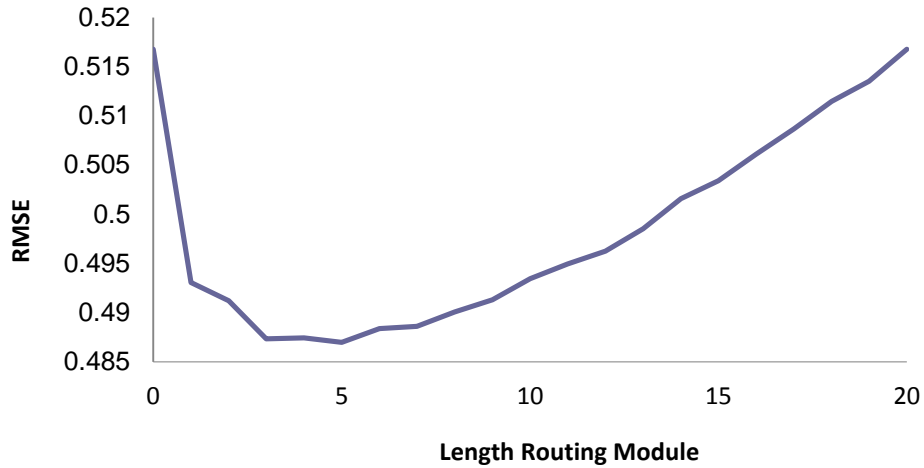
But: fewer items available for targeted modules



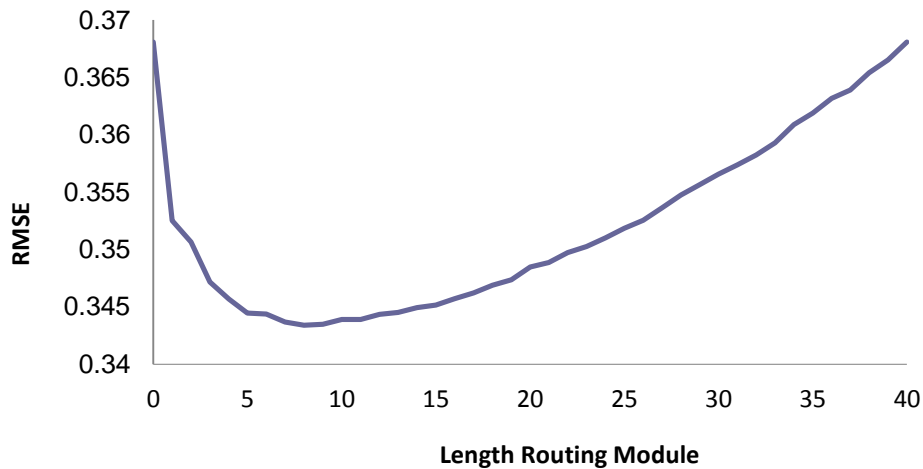
now you know

# Routing Module Length (2)

## Test length 20



## Test length 40

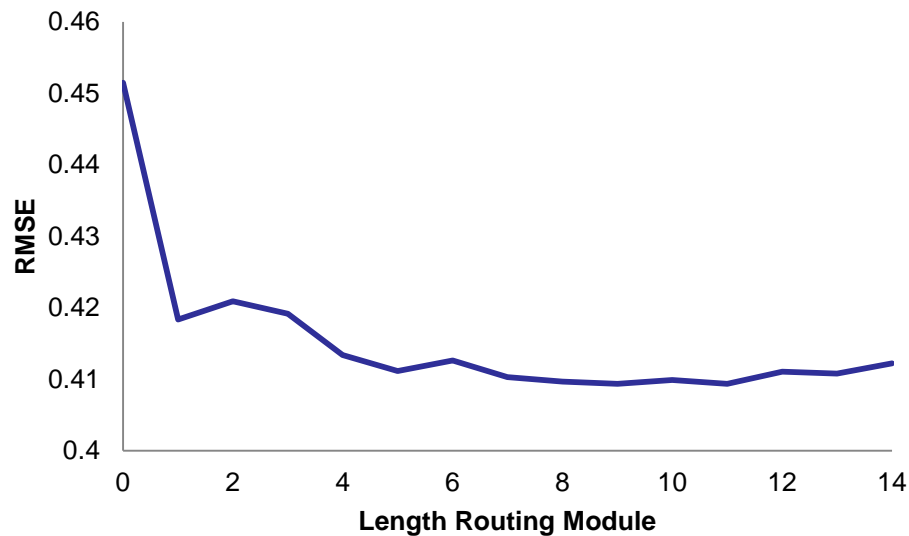


# A real life example

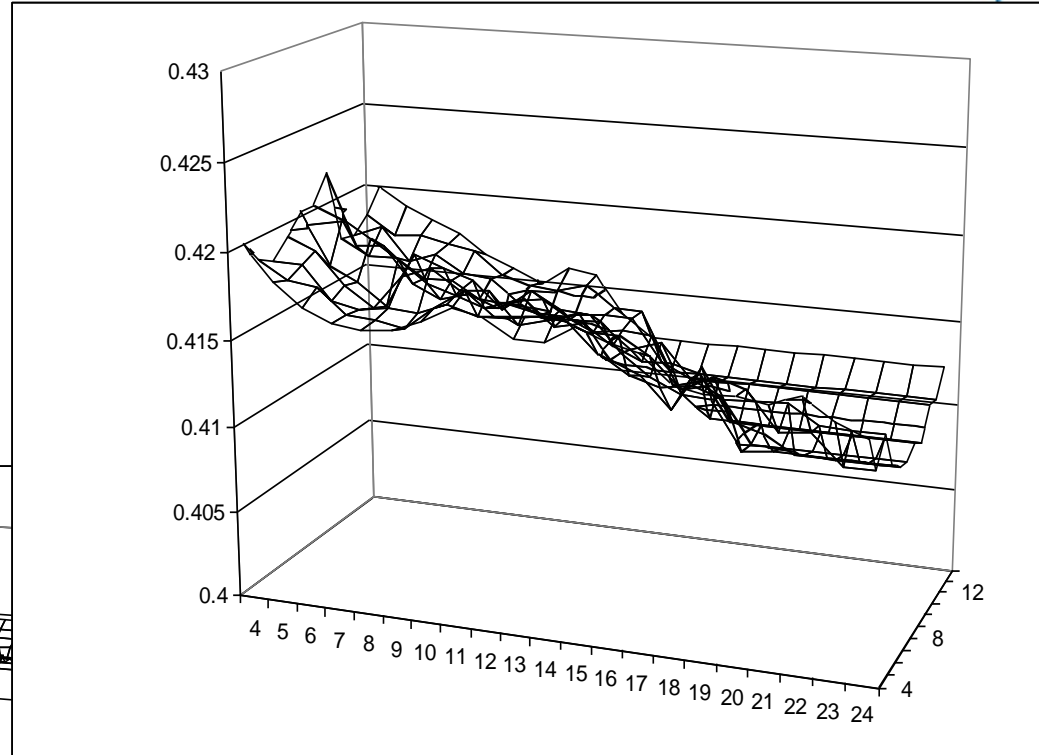
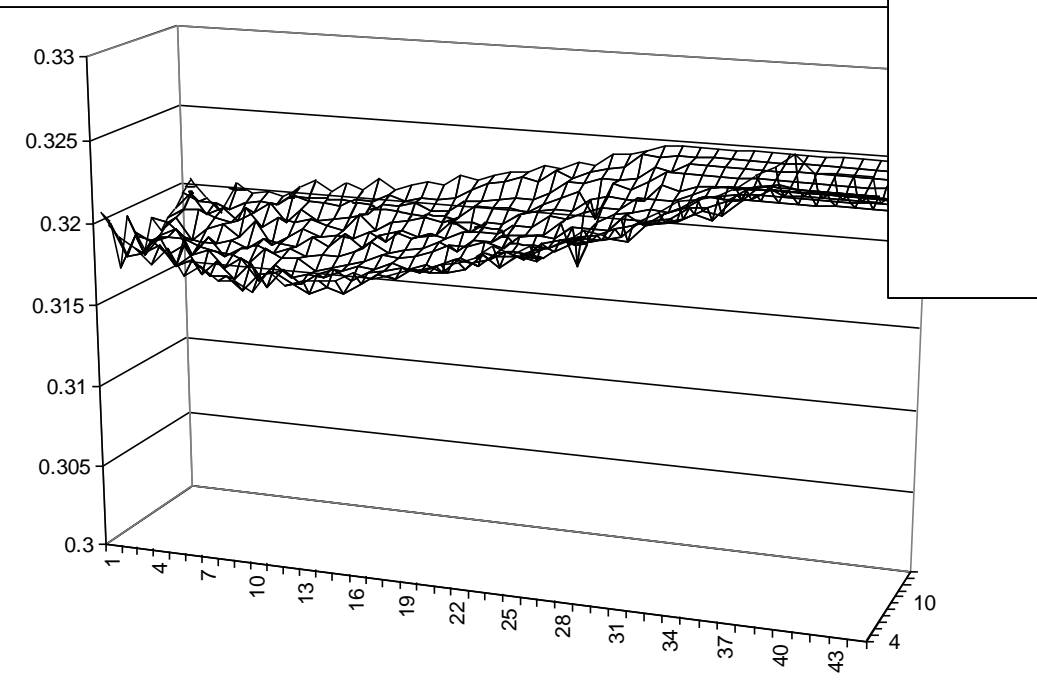
Vox: adult education, Arithmetic Test

Item pool 99 items, 2PL

Desired test length:28



# Three stages





# Conclusions

This study is just a short exploration in the matter of optimization of a MST

Extremely hard or maybe impossible to chart influence of item pool and test specifications on optimization process

Simulations are very helpful in finding an acceptable MST



now you know

# Thank you



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